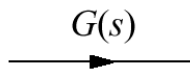


C) SIGNAL FLOW GRAPHS

- An alternative to block diagrams.
- It consists only of branches (represent system) and nodes (represents signals).
- **Branches**
 - represented by a line with arrow showing the direction of signal flow through the system

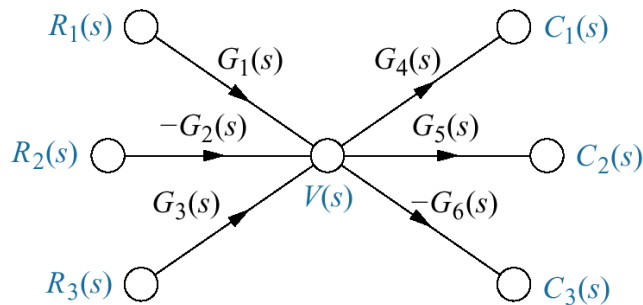


The transfer function is written close to the line and arrow

- **Nodes**
 - represented by a small circle with the signal's name is written adjacent to the node



- **Example:**



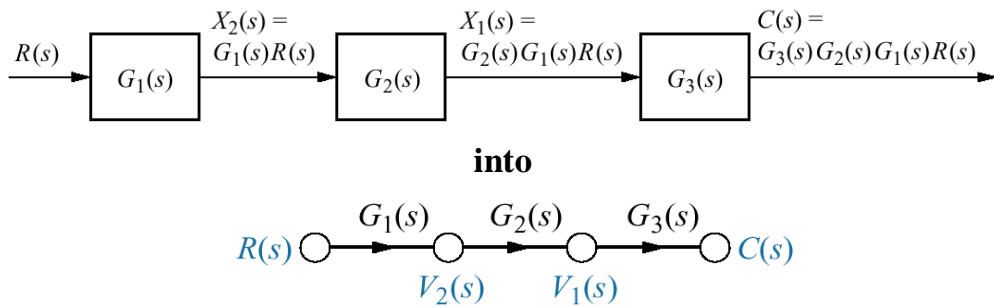
V(s)=

C₁(s)=

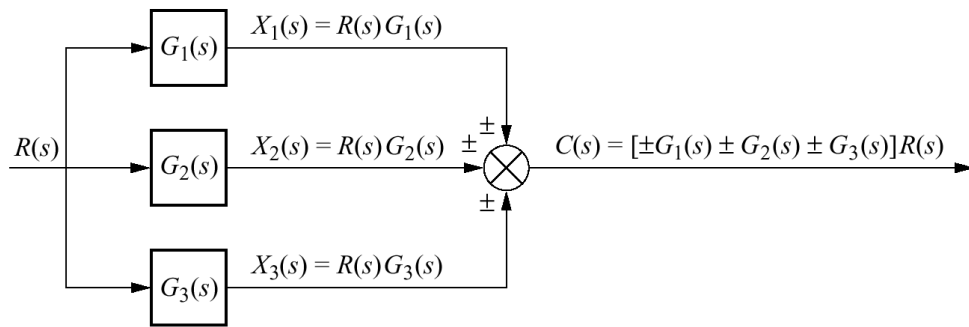
C₂(s)=

C₃(s)=

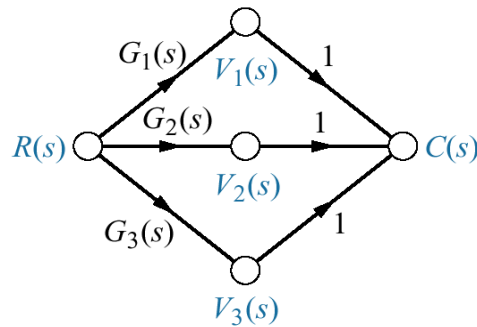
- **Converting common block diagrams into signal-flow graphs**
 - **We can convert the block diagrams in cascade, parallel and feedback forms into signal-flow diagrams**
 - **We can start with drawing the signal nodes, and then interconnect the signal nodes with system branches.**
 - **Cascade form:**



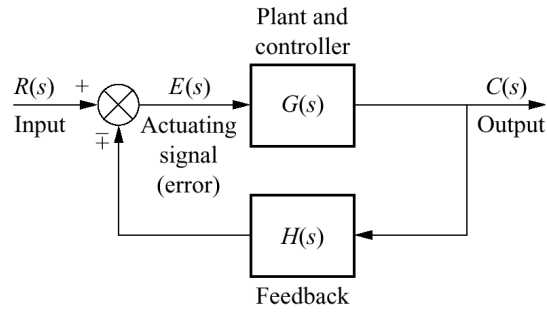
- **Parallel form:**



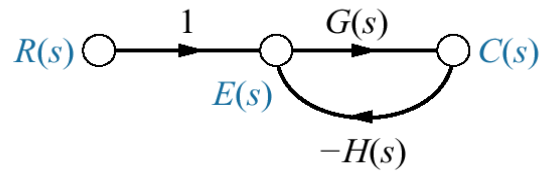
into



- **Feedback form:**

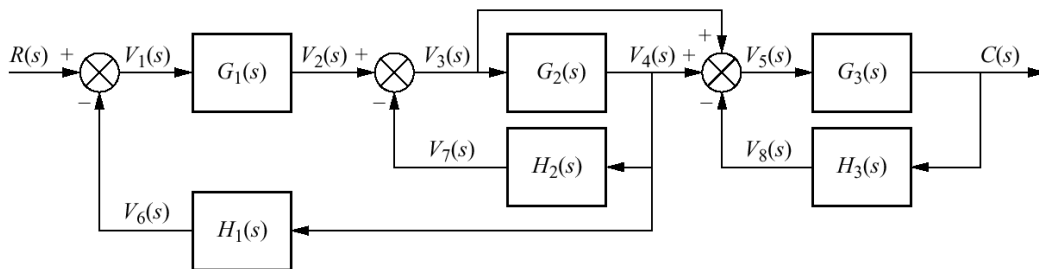


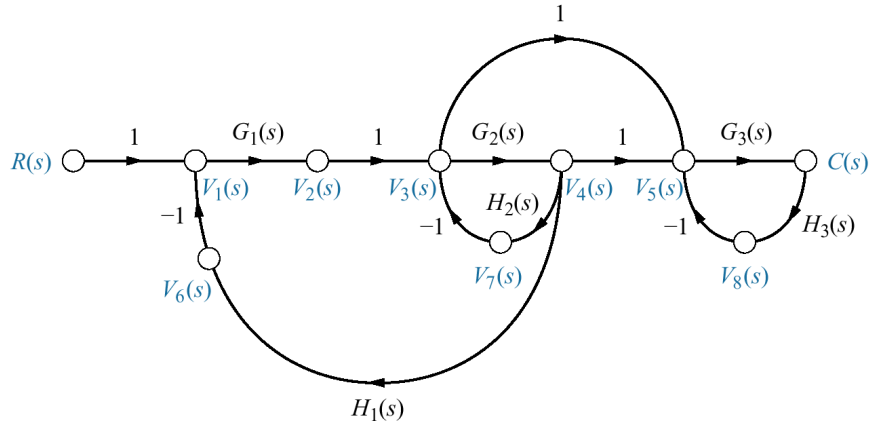
into



- **Example:**

Convert the following block diagram into signal-flow graph

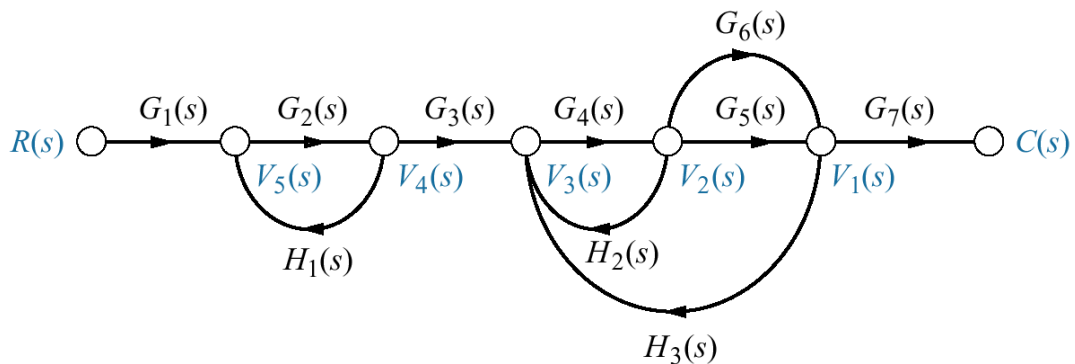




- Further example: Convert those block diagrams in previous example in the previous section.
- Make sure that the reverse (converting from signal flow to block diagram) is also possible.

D) MASON'S RULE

- Mason's rule is used to get the single transfer function in the signal-flow graph.
- We need to know some important definitions:



- Loop – a closed path which starts and ends at the same node.

- **Loop gain** – the product of branch gains found by traversing a loop.
 - $G_2(s)H_1(s)$
 - $G_4(s)H_2(s)$
 - $G_4(s)G_5(s)H_3(s)$
 - $G_4(s)G_6(s)H_3(s)$

- **Forward-path** – a path from the input node to the output node of the signal-flow graph in the direction of signal flow.

- **Forward-path gain** – the product of gains found by traversing a path from the input node to the output node of the signal-flow graph in the direction of signal flow.
 - $G_1(s)G_2(s)G_3(s)G_4(s)G_5(s)G_7(s)$
 - $G_1(s)G_2(s)G_3(s)G_4(s)G_6(s)G_7(s)$

- **Non-touching loops** – loops that do not have any nodes in common.
 - $G_2(s)H_1(s)$ is not touching with $G_4(s)H_2(s)$, $G_4(s)G_5(s)H_3(s)$ and $G_4(s)G_6(s)H_3(s)$

- **Non-touching loops gain** – the product of loop gains from non-touching loops taken two, three, four, or more at a time.
 - $[G_2(s)H_1(s)][G_4(s)H_2(s)]$
 - $[G_2(s)H_1(s)][G_4(s)G_5(s)H_3(s)]$
 - $[G_2(s)H_1(s)][G_4(s)G_6(s)H_3(s)]$

- **Mason's rule**

$$G(s) = \frac{C(s)}{R(s)} = \frac{\sum_k T_k \Delta_k}{\Delta}$$

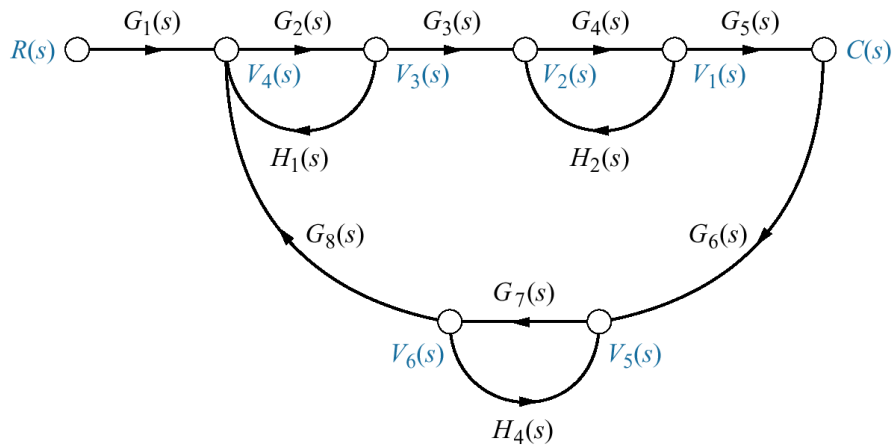
k = number of forward path

T_k = the k th forward-path gain

$\Delta = 1 - \Sigma$ loop gains + Σ non-touching loops gain (taken 2 at a time) - Σ non-touching loops gain (taken 3 at a time) + Σ non-touching loops gain (taken 4 at a time) - ...

$\Delta_k = \Delta - \Sigma$ loop gain terms in Δ that touch the k th forward path. (In other words, Δ_k is formed by eliminating from Δ those loop gains that touch the k th forward path)

- **Example: Find the transfer function, $C(s)/R(s)$ of the following signal-flow graph,**



- **Forward-path gains**

- **Loop gains**

- **Nontouching loop gains – two at a time**

- **Nontouching loop gains – three at a time**

- Δ

- Δ_k

- **The transfer function by Mason's Rule:**